# Cryptoanalysis on Zhou et al.s' User Authentication Scheme

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#### **Summary**

In this paper, we show that the end-to-end security protocol for mobile communications with end-user identification authentication due to Zhou et al. [1] has a serious flaw, it suffers from the impersonation attack. The protocol cannot achieve the claimed security.

#### 1. Introduction

Diffie-Hellman key agreement protocol [2] is a famous scheme that two parties can establish a common secret session key over an insecure network. However, it does not authenticate the other party, thus suffers from the main-in-the-middle attack. In 1997, Pack [4] first discussed the certificate based protocols for wireless mobile communicate systems. In 2004, based on [4], Chang et al. [3] propose a certificate-based authentication combined with a session key agreement protocol. In their scheme, the session key agreement protocol is based on the Diffie-Hellman key exchange protocol. In 2005, Zhou

et al. [1] pointed out that Chang et al.'s scheme is vulnerable to the impersonation attack, and proposed an improved scheme to prevent this security flaw. However, after our analysis, we find that Zhou's protocol is still insecure against the impersonation attack as well. We will show that by presenting a simple but powerful attack against their protocol.

The structure of this article is as follows. In section 2, we brief review Zhou et al.'s scheme. In section 3, we show the weakness found. Finally, a conclusion is given in section 4.

## 2. Review of Zhou et al.'s protocol

In a typical mobile communication system (e.g., GSM), communication between two mobile stations (MS) is usually established with the aid of two base stations (BS). It is usually that both the subscriber account information and the personal certificates of the

mobile users are stored in the Subscriber Identity Module (SIM) card. Several parameters in Chang et al.'s protocol [3] which are also used in Zhou's protocol [1] are discussed as follows:

Let g be a generator of the multiplicative group  $Z_p^*$ , where p is a prime, and both g and p are made public. The private key of MS is  $X_M \in Z_p^*$  and the public key is  $Y_M = g^{-X_M} \mod p$ . Similarly, the private key and public key of BS are  $X_B \in Z_p^*$  and  $Y_B = g^{-X_B} \mod p$ , respectively. For simplicity, we will omit the operator "mod p" henceforth. The certificates of both MS and BS are represented in the following.

where  $h(ID_i, R_i, data_i)S_{CA}$  means the hash value is signed by a CA's private key,  $S_{CA}$ . Both the private key  $X_M$  and the certificate  $Cert_M$  of user M are stored in the SIM card. They wished their protocol [3] to be a perfect protocol. However, in 2005, Zhou et al. [1] pointed out that their protocol is insecure. Besides, they also proposed an improvement. In the following, we only show Chang et al.'s protocol in figure 1 and omit the details.

As for Zhou's protocol, we describe it as follows and illustrate it in figure 2.

- (1) BS randomly selects a number  $R_{B}$ , then computes  $g^{R_B}$ , and sends  $g^{R_B}$ , Cert<sub>B</sub> to MS.
- (2) MS randomly selects a number  $R_M$ , computes  $Cert\ M = (ID\ M, YM, data\ M, [h(ID\ M, YM, data\ M)S\ CA\ ])_{RM}\$  and  $sk_M = Y_B^{RM}\ (g^{RB}\ )^{-XM}$ , where the public  $Cert\ B = (ID\ B, YB, data\ B, [h(ID\ B, YB, data\ B)S\ CA\ ]),$  key of BS,  $Y_B$ , can be obtained from  $Cert_B$ . Finally, MS sends the message.

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1. BS \rightarrow MS: g^{RB+XB}, Cert B

2. MS \rightarrow BS: g^{RM+XM}, Cert M, f(sk M, [ID M, ID B])

3. BS \rightarrow MS: f(sk B, [ID B, ID M])

sk B = (Y M g^{RM+XM})^{RB} = (Y B g^{RB+XB})^{RM} = sk M
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Fig. 1. Chang's Protocol.

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1. BS 	o MS : g^{RB}, Cert 	 B

2. MS 	o BS : g^{RM}, Cert 	 M, f(2, sk 	 M, [ID 	 M, ID 	 B, g^{RM}, g^{RB}])

3. BS 	o MS : f(3, sk 	 B, [ID 	 B, ID 	 M, g^{RB}, g^{RM}])

sk 	 B = Y_{M}^{RB} (g^{RM})^{-XB} = Y_{B}^{RM} (g^{RB})^{-XM} = sk 	 M
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Fig. 2. Zhou's Protocol.

$$(1) R_{B} = 0, g^{R_{B}} = 1$$

$$g^{R_{M}}, Cert_{M}, f(2, sk_{M}, [ID_{M}, ID_{B}, g^{R_{M}}, 1])$$

$$= (g^{R_{M}})^{X_{B}}$$

Fig. 3.Impersonation attack against Zhou's protocol.

$$< g^{RM}$$
 , Certm ,  $f(2,skm,[IDm,IDB,g^{RM},g^{RB}]) >$ to BS.

(3) BS computes  $sk_B = Y_M^{RB} (g^{RM})^{-XB}$ , and uses thus session key to check the validity of  $f(2, sk_M, [ID_M, ID_B, g^{RM}, g^{RB}])$ . Finally, BS sends the message  $f(3, sk_B, [ID_B, ID_M, g^{RB}, g^{RM}])$  to MS. BS and MS can confirm each other's identity and session key after executing their protocol.

# 3. Cryptanalysis of Zhou et al.'s protocol

Although, Zhou et al. claimed that their scheme can resist against the impersonation attack. However, we still can find its mistake as illustrated in Fig. 3.

In our attack, we assume that an adversary E

- (1) The adversary E selects  $R_B=0$  and computes  $g^{R_B}=1$ , then he send 1, and Cert<sub>B</sub> to MS.
- (2) MS randomly selects a number  $R_M$ , computes  $g^{RM}$  and  $sk_M = Y_B^{RM} (g^{RB})^{-XM} = Y_B^{RM} = (g^{-XB})^{RM}$ , where the public key of BS,  $Y_B$ , can be obtained from  $Cert_B$ , then computes the hash value,  $f(2, sk_M, [ID_M, ID_B, g^{RM}, 1])$ . Finally, MS sends the message  $< g^{RM}$ ,  $Cert_M$ ,  $f(2, sk_M, [ID_M, ID_B, g^{RM}, 1]) >$  to BS.
- (3) Because  $R_B=0$ , the adversary E computes  $sk_B=Y_M^{RB}$  (  $g^{RM}$  )- $^{XB}=$  (  $g^{RM}$  )- $^{XB}$ . Then E can check to see if the received hash code  $f(2,sk_M,[ID_M,ID_B,g^{R_M},1])$  is valid using the computed session key  $sk_B$ . If it is valid, E sends

the message  $f(3, sk_B, [ID_B, ID_M, 1, g^{RM}])$  to MS.

It is obvious that E can cheat MS successfully.

Conversely, an adversary E can also successfully impersonate MS to BS in the same way. We omit the details.

#### 4. Conclusion

We have shown that the Zhou et al.'s scheme suffers from the impersonation attacks. An adversary can utilize the simple method to impersonate one party to the other.

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