

# On Reducing the Degree of Long-range Dependent Network Traffic Using the CoLoRaDe Algorithm

Karim Mohammed Rezaul and Vic Grout

Centre for Applied Internet Research (CAIR), University of Wales, NEWI, Wrexham, UK

## Abstract

Long-range dependence characteristics have been observed in many natural or physical phenomena. In particular, a significant impact on data network performance has been shown in several papers. Congested Internet situations, where TCP/IP buffers start to fill, show long-range dependent (LRD) self-similar chaotic behaviour. The exponential growth of the number of servers, as well as the number of users, causes the performance of the Internet to be problematic since the LRD traffic has a significant impact on the buffer requirements. The Internet is a large-scale, wide-area network for which the importance of measurement and analysis of traffic is vital. The intensity of the long-range dependence (LRD) of communications network traffic can be measured using the Hurst parameter. A variety of techniques (such as R/S analysis, aggregated variance-time analysis, periodogram analysis, Whittle estimator, Higuchi's method, Wavelet-based estimator, absolute moment method, etc.) exist for estimating Hurst exponent but the accuracy of the estimation is still a complicated and controversial issue. Earlier research [1] introduced a novel estimator called the Hurst Exponent from the Autocorrelation Function (HEAF) and it was shown why lag 2 in HEAF (i.e. HEAF (2)) is considered when estimating LRD of network traffic. HEAF estimates  $H$  by a process which is simple, quick and reliable. In this research we extend these concepts by introducing a novel algorithm for controlling the long-range dependence of network traffic, named CoLoRaDe which is shown to reduce the LRD of packet sequences at the router buffer.

## Keywords:

*Self-similarity, LRD, ACF, HEAF(2), CoLoRaDe.*

## Introduction

The importance of Long-Range Dependence (LRD) in traffic engineering problems, such as traffic measurement, queuing behaviour and buffer sizing, admission control and congestion control, is vital. The research in [2] shows that the consequences of LRD are packet delays and application level delays that cause a heavy-tailed distribution. TCP estimates the round trip timer values from the peer acknowledgements and as a result congestions appear more frequently while maintaining the impulsive behaviour with increase in load. The influence of LRD properties on the delay performance at packet and application level is reported in [3] and metrics of network performance, such as throughput, packet loss, latency and buffer occupancy levels, are affected by the presence of LRD phenomenon across many types of networks. The work in [3] also claims that packet delay behaviour tends to be more heavy-tailed in the case of LRD traffic while the congestion window size is increased. The impact of LRD on quality of service

(QoS) has been analysed in [4] showing that, the greater the LRD, the lower the QoS.

The LRD property of traffic fluctuations has important implications on the performance, design and dimensioning of the network [5]. A simple, direct parameter, characterizing the degree of long-range dependence, is the *Hurst parameter*. The Hurst exponent (or Hurst parameter,  $H$ ), which more than a half-century ago was proposed for analysis of long-term storage capacity of reservoirs [6], is used today to measure the intensity of LRD in network traffic. A number of methods have been proposed to estimate the Hurst parameter. Some of the most popular include the aggregated variance time (V/T) [7], Rescaled-range (R/S) [5, 6], Higuchi method [8], wavelet-based method [9, 10] although there are many others. In all these methods,  $H$  is calculated by taking the slope from a log-log plot. Over time, the wavelet-based Hurst parameter has acquired popularity in estimating LRD traffic. However the study [11] explored the advantages and limitations of wavelet estimators and found that a traffic trace with a number of deterministic shifts in the mean rate results in a steep wavelet spectrum, which leads to an overestimate of the Hurst parameter. The intensity of long-range dependence is measured for file size or document size [12], packet counts (number of packets per unit time) [13, 14, 15], inter-arrival time [16, 17], frame size [18], connection size [19], packet length [20], number of bytes per unit time [5], Bit or byte rate [21] amongst others.

This paper is organised as follows. Section 2 describes the definitions of self-similarity, long-range dependence and the autocorrelation function. Section 3 elaborates the HEAF estimator. Section 4 introduces the algorithm CoLoRaDe and its function. Section 5 depicts the complexity of the CoLoRaDe by experimental analysis. Finally we draw a conclusion and suggest future works in section 6.

## 2. Self-similarity, Long-range dependence and Autocorrelation Function

In general two or more objects having the same characteristics are called self-similarity. A phenomenon that is self-similar looks the same or behaves the same when viewed at different degrees of magnification or different scales on a dimension and bursty over all time scales. Self-similarity is the property of a series of data points to retain a pattern or appearance regardless of the level of granularity used and is the result of long-range dependence in the data series. If a self-similar process is bursty at a wide range of timescales, it may exhibit long-

range-dependence. In general lagged autocorrelations are used in time series analysis for empirical stationary tests. Self-similarity manifests itself as long-range dependence (i.e., long memory) in the time series of arrivals. The evidence of very slow, linear decay in the sample lag autocorrelation function (ACF) indicates the nonstationary behaviour [22]. The research [23] shows that Internet traffic is nonstationary.

Long-range-dependence means that all the values at any time are correlated in a positive and non-negligible way with values at all future instants. For a continuous time process  $Y = \{Y(t), t \geq 0\}$  is self-similar if it satisfies the following condition [24]:

$$Y(t) \stackrel{d}{=} a^{-H} Y(at), \quad \forall a > 0, \text{ and } 0 < H < 1 \quad (2.1)$$

where  $H$  is the index of self-similarity, called Hurst parameter and the equality is in the sense of finite-dimensional distributions.

The stationary process  $X$  is said to be a long-range dependent process if its autocorrelation function (ACF) is non-summable [25] meaning that  $\sum_{k=-\infty}^{\infty} \rho_k = \infty$

The details of how ACF decays with  $k$  are of interest because the behaviour of the tail of ACF completely determines its summability. According to [5],  $X$  is said to exhibit long-range dependence if

$$\rho_k \sim L(k)k^{-(2-2H)}, \text{ as } k \rightarrow \infty \quad (2.2)$$

where  $\frac{1}{2} < H < 1$  and  $L(\cdot)$  slowly varies at infinity, i.e.,

$$\lim_{t \rightarrow \infty} \frac{L(xt)}{L(t)} = 1, \text{ for all } x > 0 \quad (2.3)$$

Equation (2.2) implies that the LRD is characterized by an autocorrelation function that decays hyperbolically rather than exponentially fast.

LRD processes are characterized by a slowly decaying covariance function that is no more summable. When the network performance is affected by LRD the data are correlated over an unlimited range of time lags and this property results in a scale invariance phenomenon. Then no characteristic time scale can be identified in the process, they are all equivalent for describing its statistics, i.e., the part resembles the whole and vice e versa. This is why LRD is also called Self-Similarity [26].

### 3. HEAF: a ‘Hurst Exponent by Autocorrelation Function’ estimator

A new estimator has been introduced [1] by extending the approach of Kettani and Gubner [27]. As in [27], for a given observed data  $X_i$  (i.e.  $X_1, \dots, X_n$ ), the sample autocorrelation function can be calculated by the following method:

$$\text{Let } \hat{\mu}_n = \frac{1}{n} \sum_{i=1}^n X_i \quad (3.1)$$

$$\text{and } \hat{\gamma}_n(k) = \frac{1}{n} \sum_{i=1}^{n-k} (X_i - \hat{\mu}_n)(X_{i+k} - \hat{\mu}_n), \quad (3.2)$$

where  $k=0,1, 2, \dots, n$ ,

$$\text{with } \hat{\sigma}_n^2 = \hat{\gamma}_n(0). \quad (3.3)$$

Then the sample autocorrelations of lag  $k$  are given by

$$\hat{\rho}_k = \frac{\hat{\gamma}_n(k)}{\hat{\sigma}_n^2} \quad (3.4)$$

(Equations (3.1), (3.2), (3.3) and (3.4) denote the sample mean, the sample covariance, the sample variance and the sample autocorrelation, respectively). A second-order stationary process is said to be exactly second-order self-similar with Hurst exponent  $1/2 < H < 1$  if

$$\rho_k = 0.5 [(k+1)^{2H} - 2k^{2H} + (k-1)^{2H}] \quad (3.5)$$

From equation (3.5), Kettani and Gubner suggest a moment estimator of  $H$ . They consider the case where  $k=1$  and replace  $\rho_1$  by its sample estimate  $\hat{\rho}_1$ , as defined in equation (3.4). This gives an estimate for  $H$  of the form

$$\hat{H} = \frac{1}{2} + \frac{1}{2 \log_e 2} \log_e(1 + \hat{\rho}_1) \quad (3.6)$$

Clearly, this estimate is straightforward to evaluate, requiring no iterative calculations. For more details of the properties of this estimator, see Kettani and Gubner [27].

An alternative estimator of  $H$  is proposed based upon equation (3.5), by considering the cases where  $k > 1$ . Note that the sample equivalent of equation (3.5) can be expressed as

$$f(H) = \hat{\rho}_k - 0.5\{(k+1)^{2H} - 2k^{2H} + (k-1)^{2H}\} = 0. \quad (3.7)$$

Thus, for a given observed  $\hat{\rho}_k, k > 1$ , a suitable numerical procedure can be used to solve this equation, and find an estimate of  $H$ . This is denoted as a HEAF( $k$ ) estimate of  $H$ .

To solve equation (3.7) for  $H$  the well-known Newton-Raphson (NR) method is used. This requires the derivative of  $f(H)$ . Here note that  $k \neq 1$ ,

$$f'(H) = -0.5 \left\{ \begin{array}{l} (2 \log(k+1))(k+1)^{2H} \\ - (4 \log(k))(k)^{2H} + \\ (2 \log(k-1))(k-1)^{2H} \end{array} \right\} \quad (3.8)$$

Hence, the algorithm to estimate HEAF( $k$ ), for any lag  $k$ , consists of the following steps:

1. Compute the sample autocorrelations for lag  $k$  of a given data set by equation (3.4). (Note that  $X_i$  can be denoted as the number of bits, bytes, packets or bit rates observed during the  $i$ th interval. If  $X_i$  is a Gaussian process, it is known as fractional Gaussian noise).
2. Make an initial guess of  $H$ , e.g.  $H_1 = 0.6$ , then calculate  $H_2, H_3, H_4, \dots$ , successively using  $H_{r+1} = H_r - f(H_r) / f'(H_r)$ , until convergence, to find the estimate  $\hat{H}$  for the given lag  $k$ . An initial consideration is of the case where  $k = 2$  in equation (3.2); i.e. HEAF(2) is considered first.

One of the major advantages of the HEAF estimator is speed, as the NR-method converges very quickly to a root. There is no general convergence criterion for NR. Its convergence depends on the nature of the function and on

the accuracy of the initial guess. Fortunately the form of the function (i.e., equation (3.7)) appears to converge quickly (within at most four iterations) for any initial guess in the range of interest, namely  $H$  in  $(0.2, 1)$ . If an iteration value,  $H_r$  is such that  $f'(H_r) \cong 0$ , then one can face “division by zero” or a near-zero number. This will give a large magnitude for the next value,  $H_{r+1}$  which in turn stops the iteration. This problem can be resolved by increasing the tolerance parameter in the NR program. A HEAF( $k$ ), for  $k = 2, \dots, 11$ , have been considered and no difficulty in finding the root in  $(0.5, 1)$  have been encountered.

#### 4. CoLoRaDe: an algorithm for controlling LRD traffic

Figure 2 illustrates a schematic view of the operation of the CoLoRaDe algorithm at the router buffer.

Here  $P_1, P_2, P_3, \dots, P_n$  are the slots of the packet sequences.

$S_1, S_2, S_3, \dots, S_n$  are the sets constructed by shuffling the slots of the packet sequences.

$P_1S, P_2S, P_3S, \dots, P_nS$  are the blocks (groups) of the sets of the slots  $P_1, P_2, P_3, \dots, P_n$  respectively.

$(P_1S)_{\min H}, (P_2S)_{\min H}, (P_3S)_{\min H}, \dots, (P_nS)_{\min H}$  are the individual sets of packet sequences from the blocks (i.e.  $P_1S, P_2S, P_3S, \dots, P_nS$ ) which possess the minimum Hurst parameter. In other words, each block (e.g.  $P_1S$ ) consists of several sets where one of the sets possesses the minimum value of Hurst parameter.

Let us assume that the client networks (such as  $C_1, C_2, C_3, \dots, C_n$ ) are connected to the main Internet service provider (ISP) router. The packet sequences from different sources are queued at the point Q. Then the packet sequences are slotted into various length (e.g.  $N = 12, N = 25, N = 50$  etc.) sequences. Each slot of these sequences is shuffled for a particular number of times so that it has several sets. Then the Hurst parameter ( $H$ ) for each set of a slot is estimated by applying the algorithm (step 1 and step 2) given in section III. In other words,  $H$ 's have been estimated for  $P_1S$  (i.e.  $P_1S_1, P_1S_2, P_1S_3, \dots, P_1S_n$ ),  $P_2S, P_3S, \dots, P_nS$  respectively and will be scheduled to the transmitter according to  $(P_1S)_{\min H}, (P_2S)_{\min H}, (P_3S)_{\min H}, \dots, (P_nS)_{\min H}$  and finally sent out to the core network (i.e. Internet) on a FIFO basis as shown in figure. The CoLoRaDe algorithm is detailed in Figure 1.

The algorithm is implemented in Java and a sample output given in Table I. Here the impact of Hurst estimates on the queuing process can be observed. The Table in the appendix represents a sample of trace files that the CoLoRaDe algorithm uses.

#### 5. Complexity of the algorithm, CoLoRaDe

To explore the complexity of CoLoRaDe, we chose six workstations with different specifications which are represented in Table II. We investigated several lengths of packet sequences such as  $N = 1000, N = 2000, N = 3000, N = 5000, N = 10000, N = 15000, N = 20000, N = 25000, N = 30000, N = 35000, N = 40000, N = 45000$

and  $N = 50000$ . According to CoLoRaDe, these lengths of sequences have been slotted by considering a certain number of samples (NS). For instance, for  $N = 1000$ , we slot this length of sequences by  $NS = 12, NS = 25, NS = 50, NS = 100, NS = 200, NS = 500$  and  $NS = 1000$ . Similar procedures have been followed for other types of length of sequences. In our research we mainly concentrate on the time complexity of the algorithm. A router introduces delay (latency) as it processes the packets it receives. Consequently, time is a crucial factor here as we cannot accept increased delay in processing the packets. Figure 3 represents the elapsed time observed using different PC's for a particular length of packet sequences where we consider different number of samples (NS) in each slot. It is clear that smaller numbers of samples per slot in the length of packet sequences contribute to longer periods of elapsed time to execute the algorithm.  $NS = 200$  per slot gives the best performance as the algorithm takes the least time to execute in this case when using PC2, PC3, PC4, PC5 and PC6.

```
noOfSets = Number of sets
noOfSamples = number of samples (e.g. packet sequence) in a set
N = Total number of incoming samples (e.g. packet)
slot = N/noOfSamples
temp = array of samples
p = current slot
```

Pick up the certain number of packets ( $X$ ) from the router buffer that are waiting to be scheduled for transmission.

acf ()

(This function calculates the samples autocorrelation function)

1. set  $p = 1$
2. while ( $p \leq \text{slot}$ )
  - i) set **start** =  $1 + \text{noOfSamples} * (p-1)$   
set **end** =  $\text{noOfSamples} * p$
  - ii) set  $m = 0$   
for  $n = \text{start}$  to **end**  
temp[m] =  $X[n]$  // (copy all samples into **temp**)  
**m = m+1**
  - iii) for  $\text{noOfShuffle} = 1$  to  $\text{noOfSets}$ 
    - a) if not first set of samples  
then Shuffle(temp)
    - b) for  $i = 0$  to  $\text{noOfSamples}$   
setsOfShuffle[noOfShuffle][i] = temp[i]
    - c) Find acf for setsOfShuffle
    - d) **rk[] = acf** // copy acf of set of packet's sequences into rk
    - e) call Heaf(rk[], Hursts[], noOfHurstParameter)
  - iv) Find out the minimum Hurst parameter from the Hursts of all sets of samples (e.g. packet sequence)
  - v) Find the set that corresponds to minimum Hurst parameter
  - vi) Transmit the set (of the packets) that contains minimum Hurst
  - vii)  $p = p+1$  (increment of slot number)
3. Go to step 1 until the packets awaiting at the router buffer
4. End of acf ()

Heaf(rk[], Hursts[], noOfHurstParameter): this function estimates the Hurst parameter by HEAF(2) method for a given samples.

Shuffle(array): this function shuffles the set of samples

main(): this is the main method which calls acf ()

Figure 1. The CoLoRaDe algorithm

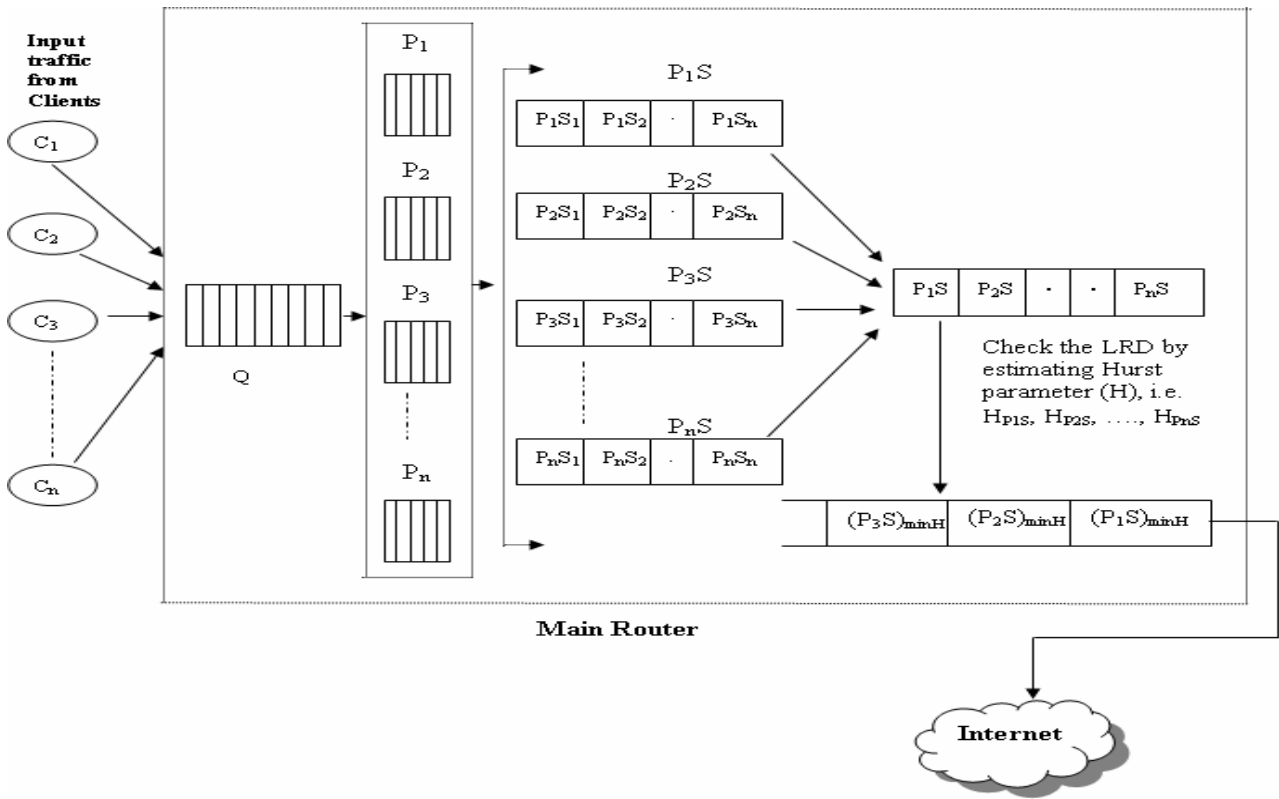


Figure 2. Illustration of packets management for controlling LRD at router buffer

TABLE I. SAMPLE OUTPUT BY COLORADE ALGORITHM

Set # 1	Set # 2	Set # 3	Set # 4	Set # 5	Set # 6
40.0	40.0	72.0	72.0	552.0	40.0
45.0	80.0	40.0	72.0	72.0	80.0
552.0	44.0	40.0	40.0	44.0	41.0
40.0	72.0	552.0	40.0	80.0	72.0
72.0	40.0	72.0	41.0	40.0	40.0
80.0	72.0	80.0	44.0	80.0	552.0
41.0	45.0	40.0	552.0	41.0	40.0
40.0	552.0	44.0	80.0	40.0	44.0
72.0	40.0	41.0	40.0	40.0	45.0
44.0	80.0	45.0	40.0	45.0	40.0
80.0	40.0	40.0	80.0	72.0	80.0
40.0	41.0	80.0	45.0	40.0	72.0

Estimated Hurst parameters for all sets are:  
 0.6654197669965659  
 0.6950803356916133  
 0.671880547095466  
 0.6465780923490018  
 0.6886795520389399  
 0.673653256908231

\*\*\* Minimum Hurst is 0.6465780923490018

The corresponding set (ready to transmit) is:  
 72.0  
 72.0  
 40.0  
 40.0  
 41.0  
 44.0  
 552.0  
 80.0  
 40.0  
 40.0  
 80.0  
 45.0

Figure 4 depicts the elapsed time for a different length of packet sequences while the performance is observed with different PC's. Number of packet sequences (NS) in each slot considered here are NS = 50, NS = 100, NS =200 and NS = 500. It is clear that PC5 outperforms for all cases as it contains higher specifications.

TABLE II. WORKSTATIONS WITH DIFFERENT SPECIFICATION

Work station	Specification
PC1	Intel Pentium (R) 4, CPU 2.4 GHz, 512 MB of RAM
PC2	Intel Pentium (R) 4, CPU 3.0 GHz, 0.99 GB of RAM
PC3	Intel Pentium (R) 4, CPU 3.0 GHz, 504 MB of RAM
PC4	Intel Pentium (R) 3, CPU 866 MHz, 384 MB of RAM
PC5	Intel Centrino Duo Core, CPU T2250 @ 1.73 GHz, 1024 MB of RAM
PC6	Intel Pentium (R) 4, CPU 1.80 GHz, 256 MB of RAM

## 6. Conclusions and Future Work

In this research we introduce a novel algorithm called CoLoRaDe to control the intensity of LRD traffic. Experimental results show that the CoLoRaDe is capable of reducing the LRD of packet sequences received at the router buffer before they are transmitted to the core network (i.e. Internet). The complexity analyses of CoLoRaDe suggest that the number of packet sequences (NS) in each set of a slot should be around NS = 200 which makes the best value to execute the algorithm

faster. To estimate the Hurst parameter, we used the process of HEAF (2) estimator (i.e. *the algorithm (step 1 and step 2)* given in section 3), which is simple, reliable and capable of yielding quick estimation. It potentially can be used for real-time traffic measurement and control at the edge routers. As the main function of the CoLoRaDe algorithm is to reduce the LRD of packet

traffic, it can contribute in reducing the network load towards the improvement of quality of service of future Internet. Future work will include evaluation of the applicability of the CoLoRaDe algorithm for real-time implementations in routers.

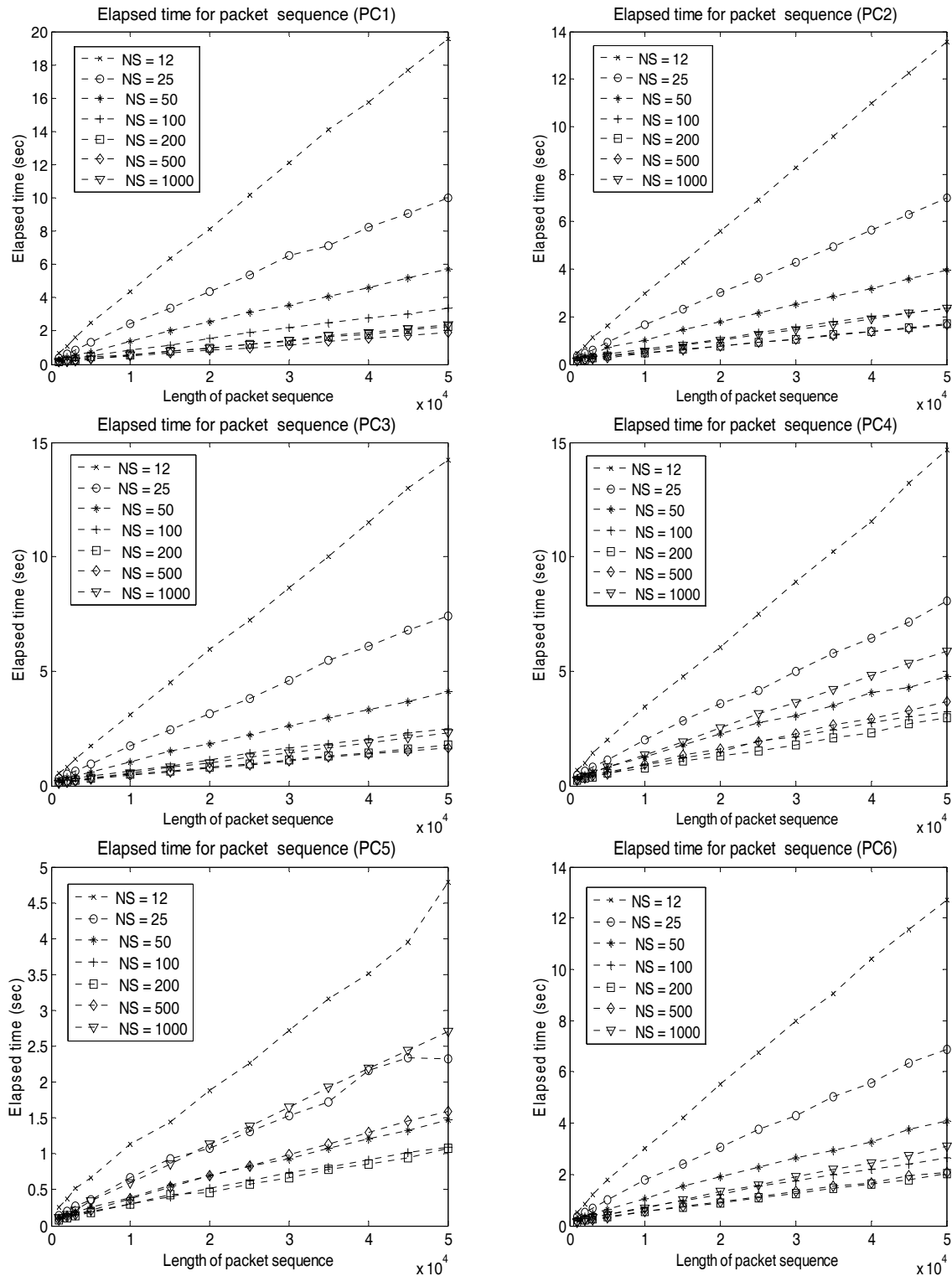


Figure 3. Elapsed time for different length of packet sequences where each block or slot contains different length of sequences (e.g. NS = 12 indicates 12 different packet sequences in each slot.)

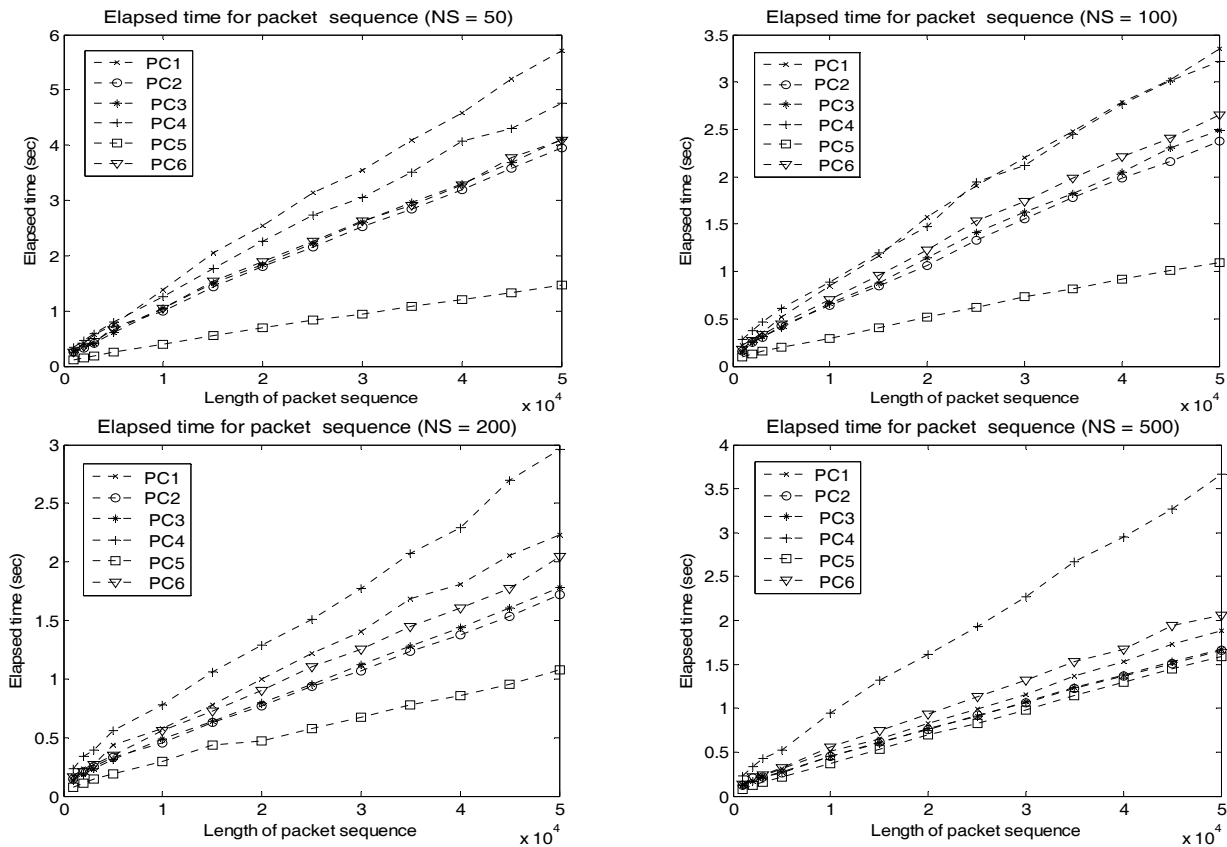


Figure 4. Elapsed time for different length of packet sequences while performance is observed with different PC's.

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## Appendix

Sample of a trace file

Length of samples	Packet size in byte ( $B_i$ )
1	41
2	42
3	42
4	41
5	82
6	55
7	41
8	42
9	42
10	454
11	40
12	95
13	55
14	40
15	40
16	41
17	41
18	104
19	41
20	72
21	84
22	552
23	79
24	104
25	44
⋮	⋮
⋮	⋮
N	$B_n$



**Karim Mohammed Rezaul** received BSc. degree in the field of Naval Architecture and Marine Engineering from Bangladesh University of Engineering and Technology (BUET), Dhaka, Bangladesh in 1998. In 2001, he was awarded an MSc degree in Marine Technology from Norwegian University of Science and Technology, Trondheim, Norway. He is a Member of IEEE, Royal Institution of Naval Architects (RINA), UK and Institution of Engineers Bangladesh (IEB), Bangladesh.

In February 2002, Mr. Karim was appointed as visiting lecturer in the department of computing, communications Technology and Mathematics at London Metropolitan University and continued until June 2005. Now he is a visiting lecturer in the department of computing at Central College London. His research interests include Network Traffic Engineering, Statistical analyses of data, Heavy tail distribution of network traffic, Long-range dependent network traffic, Modelling network traffic by Fractal and wavelet method, Traffic control mechanism and Stochastic process and probability distribution.



**Vic Grout** was awarded the BSc(Hons) degree in Mathematics and Computing from the University of Exeter (UK) in 1984 and the PhD degree in Communication Engineering from Plymouth Polytechnic (UK) in 1988.

He has worked in senior positions in both academia and industry for twenty years and has published and presented over 100 research papers. He is currently a Reader in Computer Science at the University of Wales NEWI,

Wrexham in the UK, where he leads the Centre for Applied Internet Research (CAIR). His research interests and those of his research students span several areas of computational mathematics, particularly the application of heuristic principles to large-scale problems in network design and management.

Dr. Grout is a Chartered Engineer, Chartered Scientist, Chartered Mathematician and Chartered IT Professional, a Member of the IMA, , ACM, IEEE Computer and Communications Societies, a Senior Member of the IEEE and a Fellow of the Institute of Engineering and Technology (IET) and the British Computer Society (BCS). He chairs the biennial international conference series on Internet Technologies and Applications (ITA 05 and ITA 07).