# Face recognition system using fringe projection and moiré: characterization with fractal parameters

Diana Calva Méndez<sup>1,2</sup>, Sergio Calva Méndez<sup>3</sup>, Alejandro Landa Quezada<sup>1</sup>, Heiko Rudolph<sup>4</sup> and Mario Lehman<sup>1</sup>,

CEMINT, A.C., Lisboa 14-A, Col. Juárez, México DF, MEXICO
 CADIT, Universidad Anáhuac México Norte, Estado de México, MEXICO
 Microsoft Research Silicon Valley, 1288 Pear Avenue, Mountain View, CA, 94043, USA
 RMIT University, GPO Box 2476V, Melbourne, Victoria 3001, AUSTRALIA

#### **Summary**

We show a new method for face recognition which combines the projection of structures with different characteristics (fringes, bars or grids, dots or speckle) over the face. These projections will then allow the creation of a computer-generated moiré pattern over which different kinds of fractal and complex geometry parameters are then measured. Such parameters will then be used as inputs for a neuro-symbolic hybrid system. Here, we analyze the incidence of some parameters on the efficience for the face recognition method.

#### Key words:

Face recognition, moiré structure, fractal geometry, complexity,, hybrid system..

# 1. Introduction

Moiré effect [1-3] and fringe projection [4,5] has been broadly studied by several authors, and we can also find in the literature numerous applications of these studies. Basically, the moiré effect is obtained as a pattern of clearly visible fringes when two or more structures (for example grids or diffraction gratings) with periodic geometry are superimposed. It has also been verified that the obtained fringes are a measure of the correlation between both structures [3]. Additionally, it has been shown that the moiré effect can be obtained when other types of structures are superimposed, such as random and quasi-periodic ones [6,7] or fractals [8-10]. Fringe projection entails projecting a fringe pattern or grating over an object and viewing it from a different direction. It is a convenient technique for contouring objects that are too coarse to be measured with standard interferometry. A simple approach for contouring is to project interference fringes or a grating onto an object and then view it from a different direction.

Both, moiré and fringe projection also have applications in biometric analysis [11-13], where the main objective is to achieve identification of a person, depending on their physiognomy or behavior [14]. In the same way the topography of a surface is studied, the moiré pattern can be obtained from the surface of a face by projecting structures (fringes, dots, speckle) over it. This will give us an idea of the face geometry.

Some of the tools used in face recognition are artificial neural networks [15-16] and fractal geometry [17-19], which have been used in applications related with finding specific areas of a face, or for changing its characteristics in terms of fractal dimension. Our interest in the present work is to develop a new approximation in face analysis, by using basically fractal analysis and moiré effect as inputs for an artificial neural network.

The advantage of the proposed method is that it can be combined with the measurements obtained with other known methods, but allowing this way, the use of fractal parameters.

Figs. 1(a) y 1(b) show different types of moiré obtained for the case of grids and dots respectively, both are distributed in a periodic way. This can also be applied for the case of random distributions.

As we pointed out, the main objective of the present work is the application of fractal parameters, combined with moiré and/or fringe projection. These fringes can even have fractal geometry, in which case, the variation in the fractal dimension with respect to the projection over a plane is shown. Moiré can be obtained from different structures, but we mainly show the result for the case of dots distribution. Also, generalized entropy will be considered for a complex analysis of the image of the face directly obtained with an imaging system.

Our intention is to take advantage of all the mentioned parameters in order to implement a hybrid neuro-symbolic system, where they will be used as inputs in order to make comparisons with images stored in a database. In this work, we will study the incidence of these complex parameters when using a simple neural network (perceptron multilayer).

# 2. Acquisition and image processing

Here, we consider the capture of a 3D image of a face then, the application of some of the already known methods for face recognition [20,21] are applied, afterwards a clusterization is performed based on the use of generalized entropy (Renyi [22] and Tsallis [23]). Then, the proposed method is applied. Fig. 2 shows a block diagram representing the sequence of the procedures involved in the proposed face recognition system.

First, a structure than can form moiré patterns or that can be used in 3D image processing, is projected over a face. The examples considered in the present work are fringes which can be obtained with an interferometer, as well as distributed bars, grids or dots obtained by different methods (high resolution photography or holography), or even speckle generated from a laser beam or a random mask.

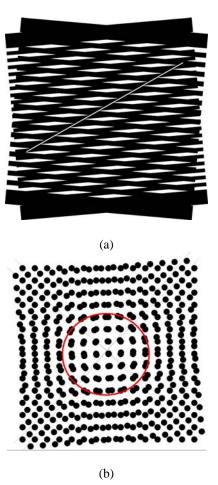


Figure 1 – Moire obtained for: (a) periodic grids, (b) dots with periodic distribution.

This way, a 3D image of the face is obtained, that can allow a parallel processing performed by the already known methods, as shown in Fig. 2. This means, that in both cases a system for the visualization of the image is available, for capturing the image from different angles, or by using a 3D scanner. With the support of image processing techniques, the image is filtered in order to obtain a deformed version of the projected dots distribution. Afterwards, a pattern is obtained by superimposing the original distribution with its deformed version, for the case of the different types of structures mentioned before. This is known as computer-generated moiré, which has already been applied for face recognition [24].

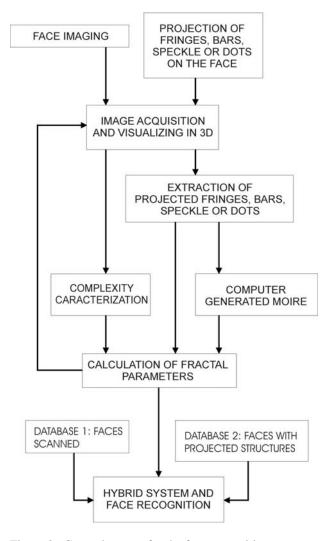


Figure 2– General system for the face recognition.

Different fractal parameters are calculated for the image of the face with and without the projected structures and for the image with a computer-generated moiré [25]. This means that fractal parameters can be calculated by three means. Over the image, with the projected structure, in which case, changes in such parameters with respect to the projection over the plane will be evaluated; another option is through the computer-generated moiré structure; and finally it can be calculated by using complexity considerations, that in our case will be calculating Renyi and Tsallis entropies in a way similar to the one used in a previous work [26]. In this case clusters are formed when particular portions of the face are taken, which can also be useful for making corrections in the image caused by lack of illumination or focus issues in the original image. As shown in Fig. 2, this will lead again to adjust the image acquisition system so that these parameters could be used for image correction or obtaining more details.

This information will be the input to the neurosymbolic hybrid system, which performs the classification.

Matching of the face of a certain person with its corresponding image is done by comparing images contained in two databases. One of them is the MIT-CBCL Face Recognition Database [27], the other one was generated for the present work (containing the projection of structures over the faces). These cases of fringe projection were obtained by a simulation over de faces in the database, for different angles and by using different characteristics for the projected structures. After obtaining the results from these projected fringes the corresponding calculations were performed, and also the moiré structures were obtained.

The difference between the proposed method, and the already existing ones, is that the projected structure or the parameters used over the obtained moiré have fractal characteristics. The following parameters can then be calculated for the pattern: generalized fractal dimension (box-counting, information and correlation included) [28], perimeter – area relation, lacunarity and succolarity [29], Tsallis [22] and Renyi [23] entropies.

We now include some definitions for the used parameters:

- Generalized dimension. If we define  $S_q^R$  as the Renyi entropy with order q, for a linear parameter  $\varepsilon$ , we have:

$$D_{q} = -\lim_{\varepsilon \to \infty} \frac{S_{q}^{R}(\varepsilon)}{\log(\varepsilon)}$$
(1)

and it can be demonstrated that  $D_{\theta}$  is the box-counting dimension,  $D_{I}$  is the information dimension and  $D_{2}$  the correlation dimension. In general,  $D_{q}$  (q>2) is the correlation dimension of order q.

- Correlation dimension: This parameter estimates the average number of data points within a radius r of the data point y(n). The quantity C(r) is defined by:

$$C(r) = \frac{1}{NM} \sum_{k=1}^{M} \sum_{n=1}^{N} \theta \left[ r - \left| y(k) - y(n) \right| \right]$$
(2)

where  $\theta$  is the Heaviside function:

$$\theta[r] = \begin{cases} 0 & r < 0 \\ 1 & r \ge 0 \end{cases} \tag{3}$$

where N and M are the elements for a matrix of pixels. The correlation dimension is defined as:

$$D_{corr} = \lim_{r \to 0} \frac{\log C(r)}{\log r}$$
(4)

- Perimeter – area relation:

$$A \approx P^{\frac{2}{D}} \tag{5}$$

where A is the area, P the perimeter of the fractal set and D is the perimeter/area dimension.

- Tsallis entropy. For an index q and a probability distribution  $P_i$ :

$$S_q^T = \frac{1}{q - 1} \left[ 1 - \sum_{i=1}^N P_i^q \right]$$
 (6)

- Renyi entropy. For an index q and a probability distribution  $P_i$ :

$$S_q^R = \frac{1}{1-q} \log \left[ \sum_{i=1}^N P_i^q \right]$$
 (7)

# 3. Moire and fringe projection

In this type of techniques, a grid with dark and clear bars or an interferometric array is used. The topography of a surface can be studied from these methods and is a very well known technique. We now show the expression for the calculation of heights for the topography methods using moiré and fringe projection. [30,31].

The equations for describing the contours of projected fringes onto a surface are given by:

$$C = \frac{\lambda}{2\sin(\Delta\theta)\sin\alpha}$$
 (8)

where  $\lambda$  is the wavelength,  $\alpha$  is the angle where the fringes are viewed and  $\Delta\theta$  the angle between the two interfering beams. In this work we present, for the first time, the projection of fringes with fractal geometry, as well as dots projection, which can be extended to speckle projection. In the first case, a variation of the fractal dimension, this can easily be deduced from the definition of generalized dimension. In the second case, a change in the correlation integral exists, and therefore, we can expect that the formed moiré superposition in such case will lead to a variation in the correlation dimension (q=2).





Figure 3 – Original face and fringes projection with periodic distribution.

# 4. Results obtained

As a first step, the methodology was tested with and experimental array by using a mannequin Fig. 3 shows an example over a face, as well as the distribution of periodic fringes projected in order to make different considerations and perform the moiré superposition. Fig. 4 shows the Cantor fringes projection, where the fractal dimension has changed from  $1.683\pm0.008$  (when projected over a plane) to  $1.474\pm0.006$  (when projected over a face). This shows the important variation that exists, and the importance of using this parameter as one of the inputs for a hybrid system.

Once tested, the methodology was implemented over the faces of the mentioned database by using computer simulation for generating and projecting the fringes in a similar way as was done with the mannequin as can be seen in Figs. 3 and 4. This way a second database was obtained containing the faces with fringe and dot projection in order to test the method.

The implementation of the method used a multilayer perceptron since it has proven its effectiveness in classification tasks. The neural network was trained with 60 examples of each class (person) and at least 10 different classes were used. Finally the neural network gives as an output the identified face.

In the case of dot projection, the distribution of the dots can be studied in terms of their size and density. The final system is then able to identify different people based on the fractal characteristics of each face, the projected structures and the generated moiré pattern

In the obtained results, the system has demonstrated being highly precise, since it uses a very robust method for the calculation of parameters and processing based on a neural network. For these developments we used the NeuroSolution (for structuring the neural network) and Benoit (for calculating the fractal dimension) software, as well as other software developed by us with Microsoft .net. Basically two types of projected structures were used: fringes and dots. The efficiency of the method varies according to different characteristics that still need to be studied and it ranges from 70% to 80%, however once the system is implemented as shown in Fig. 2, we can expect to obtain a highly efficient system.

In Fig. 5 we show the variation of the correlation dimension (calculated over the surface of a face) with the angle for a window over the image, where the superposition of dots was considered for the same face with a different one. If the registered face by the image acquisition system corresponds with one in the database, a peak of correlation exists (black line), while this is not seen for the case of different faces (red line). In the same way, as mentioned before, there exists a change in the fractal dimension when fringes with fractal structure were

projected over the faces. These parameters were then used as inputs for the neural network.





Figure 4 – Projection of Cantor fringes and random dots distribution.

Regarding face characterization by using complexity parameters (Renyi and Tsallis entropies) and fractal dimensions (box-counting and perimeter/area relation)

[32-34], we have also arrive to good results by taking different portions of the images, and focalizing in a specific zone. When comparing with images already stored in a database the results mentioned before increases around 90%.

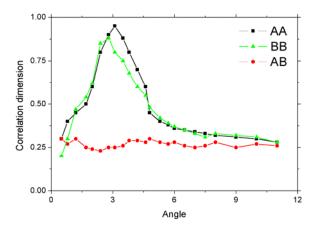


Figure 5 – Correlation dimension as a function of the angle rotation between both 3D distributions.

# 5 Conclusions and future developments

We have developed a robust system that uses image processing, fringes projection, fractal parameters, and computer-generated moiré, for sending several data as inputs for a hybrid neuro-symbolic system, which performs face recognition tasks. This method is new and we present it here for the first time. In its more general form, it combines the traditional methods for 3D characterization by using fractal geometry. It also, considers the use of some image processing techniques by using such parameters. Also, complexity parameters such as Renyi and Tsallis entropies allow the clusterization of a portion of the image which can be compared with a face database (MIT-CBCL).

In future works, we will introduce the study of generalized entropy and clustering, as well as the study of textures. We will also develop a database containing faces over which fringes, dots, and other structures have been projected and that can form moiré patterns. Also, several tests related to gestures and how they relate with changes in the fractal dimension on a still face will be performed.

### Acknowledgments

This work was supported by Centro Multidisciplinario de Ingeniería y Tecnología, CEMINT A.C.

### References

- [1] Patorski K, Kujawinska KM Handbook of Moiré Fringe Technique, Amsterdam: Elsevier, 1992.
- [2] Amidror I. The theory of the moiré phenomenon, Dordrecht Hardbound: Luwer Academic Publishers, 2000.
- [3] Kafri O, Glatt I. The Physics of Moiré Metrology, New York: John Wiley & Sons, 1997.
- [4] Creath K, Schmit J, Wyant JC. Optical Metrology of Diffuse Surfaces, in Optical shop testing, D. Malacara (ed.), Wiley-Interscience, 2007.
- [5] Böttner T, Kästner M. The Virtual Fringe Projection System (VFPS) and Neural Networks, in Fringe 2005: the 5th International Workshop on Automatic Processing of Fringe Patterns, Wolfgang Osten (ed.), Birkhäuser, 2006.
- [6] Glass L, Moiré Effect from Random Dots, Nature 223, pp. 578-580, 1969.
- [7] Amidror I, Unified approach for the explanation of stochastic and periodic moirés. J. Electr. Imag. 12(4), 669-681 (2003).
- [8] Lehman M. Superposition of Cantor gratings II: Fractality of the moiré profiles, Optik 6 (2005) 281-287.
- [9] Escobar Torres A, Lehman M. Moiré effect in Direct and Complementary Superposition of Fractal Grids, WSEAS Trans. on Systems 10 (2004) 3254-3256.
- [10] Calva Méndez D, Lehman M. Moiré effect for the superposition of two Cantor gratings", Proceedings SPIE 4829, 334-335, 2002.
- [11] D'Amico M, Merolli A, Santambrogio GC (eds.). Three dimensional analysis of spinal deformities, IOS Press, 1995.
- [12] Andrade RA, Gilbert BS, Dawson DW, Hart C, Kozaitis SP, Blatt JH. Real-time optically processed face recognition system based on arbitrary moire contours, Opt. Eng. 35(09), pp. 2534-2540.
- [13] Bingwei L, Zhen Qiang; Wu Ling. Automatic 3-D shape analysis with the aid of moire topography, Proc. of the Annual International Conference of the IEEE/EMBS, 1988, 363-368.

- [14] Ratha NK, Govindaraju V (eds.). Advances in Biometrics, Springer, 2008.
- [15] Leeland KB. Face Recognition: New Research, Nova Science Pubs; 1st ed, 2008.
- [16] Zhang M, Fulcher J. Face Recognition Using Artificial Neural Network, Group-Based Adaptive Tolerance (GAT) Trees, IEEE Transactions on Neural Networks, Vol. 7, No. 3, Mayo 1996. pp. 555 – 567.
- [17] Kwan-Ho Lin. Automatic Human Face Recognition System Using Fractal Dimension and Modified Hausdorff Distance, Lecture Notes in Computer Science, Advances in Multimedia Information Processing — PCM 2001, Springer Berlin / Heidelberg, Vol. 2195, 2001, pp. 277-284, 2001.
- [18] Shuenn-Shyang W. Fractal Model Based Face Recognition for Ubiquitous Environments, Lecture Notes In Computer Science, Vol. 5061, Proceedings of the 5th international conference on Ubiquitous Intelligence and Computing, Springer-Verlag, 2008, pp. 746-760.
- [19] Tan T, Yan H. Face recognition by fractal transformations, Proc. of the Acoustics, Speech, and Signal Processing, Vol. 06, 1999, pp. 3537-3540.
- [20] Zhao W, Chellappa R, Rosenfeld A, Phillips PJ. Face Recognition: A Literature Survey, ACM Computing Surveys, 2003, pp. 399-458.
- [21] Gross R, Shi J, Cohn J. Quo vadis Face Recognition? The current state of the art in Face Recognition, Technical Report, Robotics Institute, Carnegie Mellon University, Pittsburgh, PA, USA, 2001.
- [22] Jumarie G. Maximum Entropy, Information Without Probability and Complex Fractals: Classical and Quantum Approach (Fundamental Theories of Physics), Kluwer Academic Pub., 2000.
- [23] Gell-Mann M, Tsallis C. Nonextensive Entropy: Interdisciplinary Applications (Proceedings Volume in the Santa Fe Institute Studies in the Sciences of Complexity), Oxford University Press, Inc., 2004.
- [24] Shiang LP, Duanfeng He. Identification system using computer generated moire, US Patent 4921278.
- [25] Asundi A, Yung KH. Phase-shifting and logical moiré, J. Opt. Soc. Am. A 8 (1991) pp. 1591-1600.
- [26] Calva Méndez D, Zuñiga Garcia MA, Duchanoy Martinez C, Reyes Salgado G, Lehman M. Urine and Copro Recognition with Generalized Entropy and Neural Networks, Int. J. of Comp. Science Net. Secur., 9 (2009) pp. 173-179.

- [27] http://cbcl.mit.edu/software-atasets/heisele/facerecognitiondatabase.html, last accessed 10 June 2009.
- [28] Grassberger P. Generalized dimensions of strange attractors, Phys. Lett. 97A, 1983, pp. 227-230.
- [29] Mandelbrot BB. The Fractal Geometry of Nature, Freeman, San Francisco, 1982.
- [30] Matsumoto T, Kitagawa Y, Adachi M, Hayashi A. Moire topography for three-dimensional profile measurement using the interference fringes of a laser, Opt. Eng. 31(12), 1992, pp. 2668-2673.
- [31] Cunwei Lu. Intensity-Modulated Moiré Topography, Appl. Opt. 38(19), 1999, pp. 4019-4029.
- [32] Kouzani AZ, He F, Sammut K. Face image matching using fractal dimension, ICIP 99. Proc. International Conference on Image Processing, Vol. 3, 1999, pp. 642 646.
- [33] Takehara T. Dimensional Structure of Emotional Facial Expression Recognition and Complex Systems, in Focus on Nonverbal Communication Research, F.R. Lewis (ed.), Nova Pubs, 2007.
- [34] Komleh HE. Fractal techniques for face recognition, PhD Tesis, Queensland University of Technology, 2004.



Diana Calva Méndez. Received the B.S. degree Biomedical Universidad Engineering from Iberoamericana (México) in 1992. During 1994-1995 she taught the course Clinical Measurements and Laboratory at the Universidad Iberoamericana, and since 1995 she has worked in different Institutions in the area of Biomedical Engineering. Actually, she is a partner

founder of the company Sofilab SACV and works as Manager of the Engineering and Technology division. She is currently taking the PhD in Industrial Engineering (with a degree in Information Technologies) at the Centro de Alta Dirección en Ingeniería y Tecnología, Universidad Anáhuac (México). Her tesis is related with intelligent systems and the information processing in biomedicine. She is a founder member of the Centro Multidisciplinario de Ingeniería y Tecnología, A.C. (CEMINT). She is interested in areas such as: intelligent systems, data minning and information security, and their applications in biomedicine, image processing and computational optics.

**Sergio Calva Méndez.** Is graduated in Computer Science from ITESM, Campus Estado de Mexico in 1995. He was chair in the area de Informatica en la Secretaria de Relaciones Exteriores de Mexico. Since 2004 he has been working for Microsoft, where he has served as a field service engineer in Mexico, Latin America and more recently Spain. He is interested in areas such as software development, biometry and visual computing.



**Quezada.** Is Aleiandro Landa graduated Farmaco-Biology in Chemistry Universidad from Autónoma de México (UNAM). He obtained his masters negree Biomedical Investigation from the Instituto de Investigaciones Biomédicas (UNAM). He has been a lecturer of virology in the Facultad de

Química (UNAM). He has also been involved in several projects related with the development of methods for the diagnosis of human rotavirus, and worked at the Instituto Nacional de Nutrición Salvador Zubirón as an associate researcher in the virology department, in Bigaux Diagnóstica as biotechnology manager, and CEO. He was also CEO in Sanofi Diagnostics Pasteur Latin America and since 1997 he is CEO and founder of Sofilab S. A. de C. V., where he is also head of a project for the development of a Laboratory Information System.



Heiko Rudolph. Completed his PhD in self-administered pain relief (Patient Controlled Analgesia - PCA) at University of Melbourne, Australia. He is interested in the direct application of electric fields and currents to the human body to speed recovery after surgery or illness. He has participated as a reviewer

for several IEEE conferences and journals. His interests range from programming (C++) and microprocessors to Complementary Medicine. Having spent a number of years working for the Australian International Development Agency (AusAID) in Laos & SE Asia, is always seeking opportunities to apply practical engineering to international development.



Mario Marcelo Lehman. Received the B.S. degree from UNICEN (Argentina) and the PhD in Physics from Universidad Nacional de La Plata (Argentina) in 1999. He was visiting scientist at the Complex Media Laboratory, at Penn University (USA), Centro de Investigación Científica y Estudios Superiores de Ensenada (CICESE, México) and Instituto Nacional de Astrofísica, Optica y Electrónica

(INAOE, México). From 2000 he is working as Director of Research and Development in the company Sofilab, with projects approved by the Consejo Nacional de Ciencia y Tecnología (CONACYT). He is a founder member of the Centro Multidisciplinario de Ingeniería y Tecnología, A.C. (CEMINT). He is interested in areas such as: networks and optical systems, computacional optics and metrology, image processing and statistical physics