Hybrid Genetic Algorithms with Great Deluge For Course Timetabling

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Summary
The Course Timetabling problem deals with the assignment of course (or lecture events) to a limited set of specific timeslots and rooms, subject to a variety of hard and soft constraints. All hard constraints must be satisfied, obtaining a feasible solution. In this paper we establish a new hybrid algorithm to solve course timetabling problem based on Genetic Algorithm and Great Deluge algorithm. We perform a hybrdised method on standard benchmark course timetable problems and able to produce promising results.

Key words:
Course timetabling, Genetic algorithms, Great deluge

1. Introduction

University Course Timetabling Problems (UCTPs) is an NPhard problem, which is very difficult to solve by conventional methods and the amount of computation required to find optimal solution increases exponentially with problem size. The main idea of this problem is to assign a set of lectures to rooms and time periods satisfying a number of constraints. The set of constraints are usually divided in two sets: hard constraints and soft constraints. Hard constraints have a higher priority than soft. The objective of this problem is to satisfy the hard constraints and to minimise the violation of the soft constraints. It is therefore necessary to use efficient search methods to produce optimal or near optimal timetable that satisfy the constraints.

A large number of diverse methods have been already proposed in the literature for solving timetabling problems. These methods come from a number of scientific disciplines like Operations Research, Artificial Intelligence, and Computational Intelligence [1], [2], [3], [4], [5], [6] and can be divided into four categories:

1) Sequential Methods, that deals timetabling problems as graph problems. Generally, they order the events using domain-specific heuristics and then assign the events sequentially into valid time slots in such a way that no constraints are violated for each timeslot [7].
2) Constraint Based Methods, according to which a timetabling problem is modeled as a set of variables (events) to which values (resources such as teachers and rooms) have to be assigned in order to satisfy a number of hard and soft constraints [8].
3) Cluster Methods, in which the problem is divided into a number of events sets. Each set is defined so that it satisfies all hard constraints. Then, the sets are assigned to real time slots to satisfy the soft constraints as well [9].
4) Meta-heuristic methods, such as genetic algorithms (GAs), simulated annealing, tabu search, and other heuristic approaches, that are mostly inspired from nature, and apply nature-like processes to solutions or populations of solutions, in order to evolve them towards optimality [1], [3], [4], [10], [11], [13],[14].

Since then, the literature has hosted a large number of papers presenting evolutionary methods and applications on such problems with significant success [12].

The paper is organised as follows, the next section introduces the university course timetable problem with a set of all hard and soft constraints. In section 3 we represent the main concepts about Genetic algorithm. Section 4 introduces the great deluge algorithm. Hybridization between genetic algorithms and great deluge are represented in section 5. The simulation results are represented in section 6, and finally conclusion and future work are represented in section 7.

2. Problem description

The general timetable problem can be expressed in the following way: a number of events must be timetabled by associating them with timeslots. In university course

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timetable, a set of events (courses) is scheduled into a fixed number of rooms and timeslots within a week. In this paper, we test our method on the problem instances introduced by Socha et al [13]. The problem presents a set of N courses to be scheduled in 5 days of 9 periods each, which time T = 45 timeslots, a set R rooms (each room have a set of F features and capacity), a set of M students and a set of features required by courses. Each student attends a subset of courses. Solutions in which all courses are assigned to periods and rooms and satisfy all hard constraints are called feasible solutions. The hard constraints considered for this problem are:

1) No student can be assigned to more than one course at the same time.
2) The room should satisfy the features required by the course.
3) The number of students attending the course should be less than or equal to the capacity of the room.
4) No more than one course is allowed at a timeslot in each room.

The soft constraints considered for this problem are:

1) A student has to attend only one course in a day.
2) A student has to attend more than two courses consecutively.
3) A student has to attend a course in last period in any day.

The objective of this problem is to satisfy the hard constraints and to minimise the violation of the soft constraints.

3. Genetic Algorithms

GA is the most famous among EA algorithms. GAs have been employed as a tool that can handle multi-model function and complex search space. They have the capability to search complex spaces with high probability of success in finding the points of minimum or maximum on the search space (i.e. landscape). Genetic Algorithms (GAs) are derivative-free stochastic search algorithms. GAs applies the concept of natural selection. This idea was first introduced by John Holland at the University of Michigan in 1975 [1]. GAs have been successful used in solving numerous applications in engineering and computer science [12, 13, 14, 15]. GA gains a great popularity due to their known attributes. These attributes include:

- GAs can handle both continuous and discrete optimization problems. They require no derivative information about the fitness criterion [16, 17].
- GA has the advantageous over other search algorithm since it is less likely to be trapped by local minimum.
- GA provide a more optimal and global solution. They are less likely to be trapped by local optimal like Newton or gradient descent methods [18, 19].
- GA has been shown to be less sensitive to the presence of noise and uncertainty in measurements [5, 20].
- GAs use probabilistic operators (i.e. crossover and mutation) not deterministic ones.

Genetic algorithms code the candidate solutions of an optimization algorithm as a string of characters which are usually binary digits [23]. In accordance with the terminology that is borrowed from the field of genetics, this bit string is usually called a chromosome (i.e. individuals). A number of chromosomes generate what is called a *population*. The structure for each individual can be represented as follows:

$gene_1$	$gene_2$	$\ldots\ldots$	$gene_n$
11101	00101	$\ldots\ldots$	11011

1.

This chromosome has number of genes equal to *n*. These genes are used in the evaluation function f. Thus, $f(gene_1, gene_2, \ldots, gene_n)$ is the function to be minimized or maximized.

A. Evolutionary Process

The evolutionary process of GAs starts by the computation of the fitness of the each individual in the initial population. While stopping criterion is not yet reached we do the following:

- Select individual for reproduction using some selection mechanisms (i.e. tournament, rank, etc).
- Create an offspring using crossover and mutation operators. The probability of crossover and mutation is selected based on the application.
- Compute the new generation of GAs. This process will end either when the optimal solution is found or the maximum number of generations is reached.

- A flowchart for a simple GA process is given [21] in Figure 1

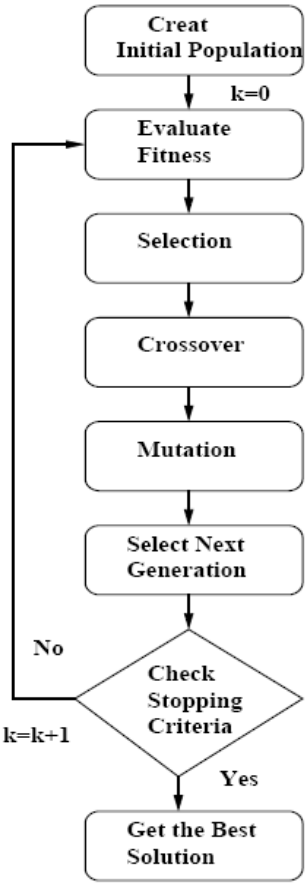

Fig. 1. Flowchart of a simple GAs process

B. SELECTION MECHANISM

Selection is the process which guides the evolutionary algorithm to the optimal solution by preferring chromosomes with high fitness. The chromosomes evolve through successive iterations, called generations. During each generation, the chromosomes are evaluated, using some measure of fitness. To create the next generation, new chromosomes, called offspring, are formulated by using some operators called crossover and mutation. Thus, a new generation will be created by selecting the best chromosomes (parents) from the previous generation and the best chromosomes from the offspring [22].

After several generations of creation the algorithm hopefully converges to the optimal solution or at least the optimal domain of solution. After computing the fitness of each individual, a new population must be created. To do this, two operators borrowed from natural genetic, crossover and mutations, are used [16, 17]. Crossover operator is used to produce new pairs of individuals from their parents. The produced individuals (i.e. childes) have many features from their parents. There is a high probability that the child's will provide a better fit to the problem.

C. CROSSOVER MECHANISM

Crossover is the main genetic operator. In [1] Holland indicates that crossover provides the main search operator while bit mutation simply serves as a background operator to ensure that all possible solutions can enter the population. The probabilities commonly assigned to crossover and bit mutation reflect this philosophical view. It operates on two chromosomes at a time and generates offsprings by combining both chromosomes' features.

One way to do crossover is to choose a random cut-point and generate the offspring by combining the segment of one parent to the left of the cutpoint with the segment of the other parents to the right of the cut-point. This type of crossover operates with the bit string representations. Single point crossover of two binary string chromosomes is presented in Figure 2.

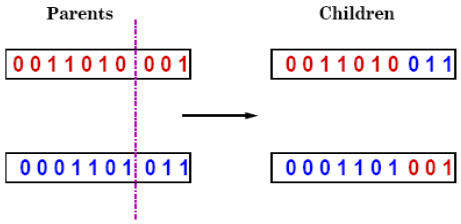

Fig. 2. Single-point crossover of two binary string chromosomes

For other types of representation other crossover types are suggested. Syswerda [23] conducted function optimization experiments with number of mutation mechanism. They include uniform crossover, two-point crossover and one-point crossover. He found that uniform crossover can provide better solutions with less computational effort.

D. MUTATION MECHANISM

Mutation is a background operator which produces spontaneous random changes in various chromosomes.

In genetic algorithms, mutation serves the role of either replacing the genes lost from the population during the selection process so that they can be tried in a new form or providing for genes that were not present in the initial population. One way to do mutation would be to alter one or more genes. In Figure 3, we show binary string chromosomes mutation.

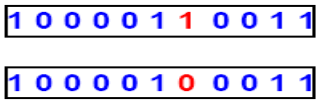

Fig. 3. Mutation of binary string chromosomes

GA evaluates the individuals in the population using a selected fitness function (criterion). This function indicates how good or bad a candidate solution is. The way to select the fitness function is a very important issue in the design of genetic algorithms, since the solution of the optimization problem and the performance of the algorithm count mainly on this function.

It is important to recognize that GAs is different from other optimization techniques like gradient descent, since they evaluate a set of solution in the population at each generation, makes them more likely to find the optimum solution.

The fitness of the individuals within the population is evaluated, and new individuals are generated for the next generation using a selection mechanism. Although convergence to a global optimum is not guaranteed in many cases, these population-based approaches are much less likely to converge to local optimal and are quite robust in the presence of noise [16, 17].

4. Great Deluge Algorithm

The Great Deluge algorithm (GD) is a generic algorithm applied to optimization problems, which was introduced by Dueck (1993) [19]. It is a local search procedure which has certain similarities with simulated annealing but has been introduced as an alternative. This approach is far less dependent upon parameters than simulated annealing. It needs just two parameters: the amount of computational time that the user wishes to "spend" and an estimate of the quality of solution that a user requires. Apart from accepting a move that improves the solution quality, the great deluge algorithm also accepts a worse solution if the quality of the solution is less than or equal the level. In this work, the "level" is initially set from EM algorithm. The GD terminate when the solution reach the estimated quality. The search continues until the bound reaches the lower limit (estimated quality). The pseudo code for our implementation of the great deluge algorithm is presented in Figure 4.

```
Set initial solution as Sol_best taken from GA
Calculate the initial cost function value,
f(Sol);
Set best solution, Sol_best ← Sol;
Set estimated quality of final solution,
estimatedquality from the user.
Set number of iterations, NumOfIte;
Set initial level: level ← f(Sol);
Set decreasing rate
    β = ((f(Sol)-estimatedquality)/(NumOfIte);
Set iteration ← 0;
Set not_improving_counter ← 0;
do while (iteration < NumOfIte)
Define neighbourhood of Sol by randomly
assigning course to a valid timeslot to
generate a new solution called Sol*;
     Calculate f(Sol*);
     if (f(Sol*) < f(Sol_best))
        Sol ← Sol*;
        Sol_best ← Sol*;
        not_improving_counter ← 0;
      else
         if (f(Sol*)≤ level)
           Sol ← Sol*;
           not_improving_counter ← 0;
         else
          Increase not_improving_counter by 1;
          if (not_improving_counter ==
             not_improving_ length_GDA)
            exit;
level = level - β;
Increase iteration by 1;
end do;
```

Fig. 4: The pseudo code for the great deluge algorithm

5. Hybrid Genetic Algorithm with Great Deluge

Figure 5 shows a pictorial illustration for the hybridization between genetic algorithms and great deluge, as shown, the sequence of our proposed method start from initial solutions. Applying genetic algorithms as a second step, finally applying great deluge mechanism to enhance the quality of solution. Great deluge is consider one of the powerful local optimization algorithm while GA is one of the best known methods of global optimization, combining both algorithms means combine the advantages of both algorithms.

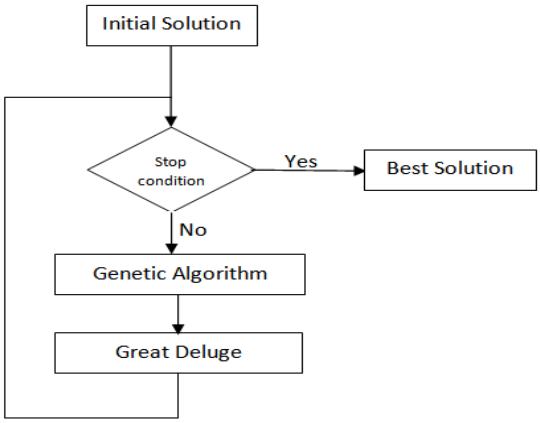

Fig.5: Pictorial Diagram for Hybrid GA with GD

6. Simulation Results

The proposed algorithm was programmed using C++ and simulations were performed on the Intel Pentium 4 2.33 GHz computer and tested on a standard benchmark course timetable problem as presented in SectionII. Table I shows the parameter for the GA algorithm chosen after some preliminary experiments, and almost similar with the papers in the literature [16], [19].

Our algorithm is capable to find a feasible timetable for all eleven cases. Table II shows the results obtained and the comparison with other approaches in the literature such as Genetic Algorithms with Local Search (GA & LS) by Abdullah et al (2008) [21], the Randomised Iterative Improvement Algorithm by Abdullah et al. (2005), a graph hyperheuristic by Burke et al. (2005), Extended Great Deluge (EGD) [22] by P. McMullan (2007) and Non-linear Great Deluge (NLGD) by (2008) [20], From Table II, it is clear that the result of our proposed algorithm produces acceptable timetables.

TABLE I
PARAMETER SETTING FOR EM ALGORITHM

Parameter	**Value**
Generation Number	100000
Population size	50
Crossover Rate	0.6
Mutation Rate	0.06
Selection Method	Roulette Wheel selection
Crossover Type	Single point

We ran the experiments for 100000 iterations for GA with population size 50. Table II shows the comparison of our final results compared to other published results in the literature.

TABLE II
COMPARISON BETWEEN VARIOUS VERSION METHODS AND OUR METHOD

Data Set	Our Method Best	GA & LS	Randomised Iterative Improvement Algorithm	Graph hyper-heuristic (Best)	EGD	NLGD
s1	**0**	2	0	6	0	3
s2	**0**	4	0	7	0	4
s3	**0**	2	0	3	0	6
s4	**0**	0	0	3	0	6
s5	**0**	4	0	4	0	0
m1	**75**	254	242	372	80	140
m2	**100**	258	161	419	105	130
m3	143	251	265	359	**139**	189
m4	180	321	181	348	**88**	112
m5	125	276	151	171	**88**	141
l	**650**	1027	-	1068	730	876

7. Conclusion

In this paper, we employed Genetic Algorithm (GA) and great deluge for course timetable problem local search. Even though the experiments carried out in this work demonstrate that the method presented here only obtains two best result, However the proposed method can produce a feasible and good quality timetable Moreover, it provides results that are consistently good across the all the benchmark problems.

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