Decision Tree Classification Implementation with Fuzzy Logic

Renuka D. Suryawanshi *, D. M. Thakore**
*Computer Engineering Department Year Bharti Vidyapeeth, Pune, India
** Computer Engineering Department Bharti Vidyapeeths Deemed University College Of Engineering, Pune, India

Summary:
Data mining is having an aim to analyze the observation datasets to find relationship and to present the data in ways that are both understandable and usable. This paper basically focuses on the classification technique of datamining to identify the class of an attribute with an ID3 (classical decision tree approach) and then to add fuzzification to improve the result of ID3. It also contains design and implementation of this combined approach with chosen datasets. Id3 results are based on information gain theory and Entropy values of each attribute. Fuzzy ID3 results are based on information gain of fuzzy dataset and fuzzy entropy. Classification results are presented as decision tree which incorporates the result of Id3 & FID3.

Keywords:
ID3(Iterative Dichotomizer 3), FID3(Fuzzy iterative dichotomizer3), CLS(Concept Learning System), IG(Information Gain)

1. Introduction

1.1 Decision Tree

In data mining and machine learning, decision tree is a predictive model that is mapping from observations about an item to conclusions about its target value. The machine learning technique for inducing a decision tree from data is called decision tree learning.[2]

'Decision tree learning is a method for approximating discrete-valued target functions, in which the learned function is represented by a decision tree. Decision tree learning is one of the most widely used and practical methods for inductive inference'.

Decision tree learning algorithm has been successfully used in expert systems in capturing knowledge. The main task performed in these systems is using inductive methods to the given values of attributes of an unknown object to determine appropriate classification according to decision tree rules.[1]

2. ID3(Iterative Dichotomizer 3)

Iterative Dichotomizer 3 algorithm [1] is one of the most used algorithms in machine learning and data mining due to its easiness to use and effectiveness. J. Rose Quinlan developed it in 1986 based on the Concept Learning System (CLS) algorithm. It builds a decision tree from some fixed or historic symbolic data in order to learn to classify them and predict the classification of new data. The data must have several attributes with different values. Meanwhile, this data also has to belong to diverse predefined, discrete classes (i.e. Yes/No). Decision tree chooses the attributes for decision making by using information gain (IG). [3]

2.1 Implementation of ID3

Here we implemented the ID3 in java as per following steps.

Step 1: we have chosen the following sample dataset as an example to show the result.

<table>
<thead>
<tr>
<th>Column 0</th>
<th>Column 1</th>
<th>Column 2</th>
<th>Column 3</th>
<th>Column 4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Male</td>
<td>0</td>
<td>Cheap</td>
<td>Low</td>
<td>Bus</td>
</tr>
<tr>
<td>Male</td>
<td>1</td>
<td>Cheap</td>
<td>Medium</td>
<td>Bus</td>
</tr>
<tr>
<td>Female</td>
<td>1</td>
<td>Cheap</td>
<td>Medium</td>
<td>Train</td>
</tr>
<tr>
<td>Female</td>
<td>0</td>
<td>Cheap</td>
<td>Low</td>
<td>Bus</td>
</tr>
<tr>
<td>Male</td>
<td>1</td>
<td>Cheap</td>
<td>Medium</td>
<td>Bus</td>
</tr>
<tr>
<td>Male</td>
<td>0</td>
<td>Standard</td>
<td>Medium</td>
<td>Train</td>
</tr>
<tr>
<td>Female</td>
<td>1</td>
<td>Standard</td>
<td>Medium</td>
<td>Train</td>
</tr>
<tr>
<td>Female</td>
<td>1</td>
<td>Expensive</td>
<td>High</td>
<td>Car</td>
</tr>
<tr>
<td>Male</td>
<td>2</td>
<td>Expensive</td>
<td>Medium</td>
<td>Car</td>
</tr>
<tr>
<td>Female</td>
<td>2</td>
<td>Expensive</td>
<td>High</td>
<td>Car</td>
</tr>
</tbody>
</table>

Step 2: Information gain and Entropy calculation

The basic ID3 method selects each instance attribute classification by using statistical method beginning in the top of the tree. The core question of the method ID3 is how to select the attribute of each pitch point of the tree. A statistical property called information gain is defined to measure the worth of the attribute. The statistical quantity Entropy is applied to define the information gain, to choose the best attribute from the candidate attributes.

The definition of Entropy is as follows:

\[ H(S) = \sum_{i=1}^{N} - P_i \cdot \log_2(P_i) \] (1)

where \( P_i \) is the ratio of class \( C_i \) in the set of examples \( S = \{ x_1, x_2, ..., x_k \} \)
Step 3: Calculating highest information gain. Now consider the above dataset shown in Table 2.1. As this algorithm is based upon information gain of each attribute with entropies. First we need to calculate the information gain for each record set according to attributes given in dataset.

(i) Calculating gain for column 0 record set:
   [Male, Male, Female, Female, Male, Male, Female, Male, Female].
   For Male: Record set: [Bus, Bus, Bus, Train, Car]
   Entropy: 0.44217935649972373
   For Female: Record set: [Train, Bus, Train, Car, Car]
   Entropy:0.46438561897747244

(ii) Getting impurity using entropy
   Record set: [Bus, Bus, Train, Bus, Bus, Train, Train, Car, Car, Car]
   Entropy: 0.5287712379549449
   Gain: 0.22108967824986187
   Gain: 0.4532824877385981
   Gain: 0.4532824877385981
   Information gain: 0.07548875021634677

As per the same way we calculated the information gain for each record set.
Below we give the calculation for each record set

Column 1:
Calculating gain for record set: [0, 1, 1, 0, 1, 0, 1, 1, 2, 2]
Information gain: 0.338082178394093

Column 2:
Calculating gain for record set: [Cheap, Cheap, Cheap, Cheap, Standard, Standard, Standard, Expensive, Expensive, Expensive]
Information gain: 0.6321928094887361

Column 3:
Calculating gain for record set:[Low, Medium, Medium, Low, Medium, Medium, Medium, High, Medium, High]
Information gain: 0.253282487738598

Step 4: Generate Information Gain Table
[0.07548875021634677, 0.338082178394093, 0.6321928094887361, 0.253282487738598]

Highest gain column: 0.6321928094887361
As per the result we get highest information gain for column no. 2
We design a decision tree based upon the results as we get the highest information gain on column no. 2. The decision tree is given below.

3. Fuzzy logic

The concept of Fuzzy Logic (FL) was given by Lotfi Zadeh, a professor at the University of California at Berkley, and presented as a way of processing data by allowing partial set membership rather than crisp set membership or non-membership (Babuska, 1998). It is basically a multi-valued logic that allows intermediate values to be defined between conventional evaluations.

3.1 Fuzzy sets

A fuzzy set is a set without a crisp and clearly-defined boundary or without binary membership characteristics. Unlike an ordinary set where each object (or element) either belongs or does not belong to the set, fuzzy set can contain elements with only a partial degree of membership. In other words, there is a 'softness' associated with the membership of elements in a fuzzy set.

An example of a fuzzy set could be ‘the set of tall people.’ There are people who clearly belong to the above set and others that cannot be considered as tall. Since the concept of ‘tall’ is not precisely defined (for example, >2m), there will be a gray zone in the associated set where the membership is not quite obvious. As another example, consider the variable 'temperature'. It can take a fuzzy value (e.g., cold, cool, tepid, warm, and hot). Each fuzzy value such as ‘hot’ is called a fuzzy descriptor. It may be represented by a fuzzy set because any temperature that is considered to represent ‘hot’ belongs to this...
A fuzzy set can be represented by a membership function. This function indicates the grade (degree) of membership within the set, of any element of the universe of discourse (e.g. the set of entities over which certain variables of interest in some formal treatment may range).

The membership function maps every element of the universe to numerical values in the interval [0, 1]. Specifically,

$$\mu_A(x) : X \rightarrow [0, 1]$$

Where $\mu_A(x)$ is the membership function of the fuzzy set $A$ in the universe $X$. Stated in another way, fuzzy set $A$ is defined as a set of ordered pairs:

$$A = \{ (x, \mu_A(x)) : x \in X, \mu_A(x) \in [0, 1] \}$$

The membership function ($\mu$) represents the extent to which an element $x$ belongs to the set $A$. It is a curve that defines how each point in the input space is mapped to a membership value. A membership function value of zero indicates that the corresponding element is definitely not an element of the fuzzy set. A grade of membership greater than 0 and less than 1 corresponds to a non-crisp (or fuzzy) membership, and the corresponding elements fall on the fuzzy boundary of the set.

The closer the $\mu_A(x)$ is to 1 the more the $x$ is considered to belong to $A$, and similarly, the closer it is to 0 the less it is considered to belong to $A$.

The following is a summary of the characteristics of fuzzy set and membership function:

1. Fuzzy sets describe vague concepts (e.g., fast runner, hot weather, and weekend days).
2. A fuzzy set admits the possibility of partial membership in it. (e.g., Friday is sort of a weekend day, the weather is rather hot).
3. The degree to which an object belongs to a fuzzy set is denoted by a membership value between 0 and 1. (e.g., Friday is a weekend day to the degree 0.8).
4. A membership function associated with a given fuzzy set maps an input value to its appropriate membership value.

4. Fuzzification to create the decision tree

Fuzzy decision tree is an extension of classical decision tree and an effective method to extract knowledge in uncertain classification problems. It applies the fuzzy set theory to represent the data set and combines tree growing and pruning to determine the structure of the tree.

In general, there exist two different kinds of attributes: discrete and continuous. Many algorithms require data with discrete value. It is not easy to replace a continuous domain with a discrete one. This requires some partition and clustering. It is also very difficult to define the boundary of the continuous attributes. For example, how do we define whether the traffic-jam is long or short? Can we say that the traffic-jam of 3 km is long, and 2.9 km is short? Can we say it is cool when the temperature is 9, and it is mild for 10?

Therefore, some scholars quote the fuzzy concept in the method ID3, substitute the sample data with the fuzzy expression and form the fuzzy ID3 method. Below is the example of the fuzzy representation for the sample data.

4.1 Fuzzy Entropy and Information Gain

Next, we have to calculate the fuzzy Entropy and Information Gain of the fuzzy data set to expand the tree.

In this case, we get the same result of the entropy of the as ID3.

The formulas of the entropy for the attributes and the Information Gain are a little bit different because of the data fuzzy expression. Their definitions are defined as follow respectively with the assumption dataset $S = \{ x_1, x_2, ..., x_i \}$

$$H_f(S,A) = -\sum_{i=1}^{C} \frac{\sum_{j=1}^{N} \mu_{ij}}{S} \log_2 \frac{\sum_{j=1}^{N} \mu_{ij}}{S}$$

$$G_f(S,A) = H_f(S) - \sum_{v \in A} \frac{|S_v|}{S} * H_f(s_v,A)$$

where:

- $\mu_{ij}$ is the membership value of the $j^{th}$ pattern to the $i^{th}$ class.
- $H_f(S)$ presents the entropy of the set $S$ of training examples in the node.
- $S_v$ is the size of the subset $S$, $S_v$ is the subset of training examples $x_i$ with $v$ attribute.
- $|S_v|$ presents the size of set $S$.

4.1.1 Calculating highest gain

Following are the calculations for fuzzy gain and entropy.

(i) Column [0]:
Calculating gain for record set: [Male, Male, Female, Female, Male, Male, Female, Female, Male, Female]

For Male:
Record set: [Bus, Bus, Bus, Train, Car] >> Entropy: 1.3709505944546687
ForFemale
Record set: [Train, Bus, Train, Car, Car]
Entropy: 1.5219280948873621
Getting impurity using entropy
Record set: [Bus, Bus, Train, Bus, Bus, Train, Train, Car, Car, Car]
Entropy: 1.570505944546684
Gain: 0.6854752972273344
Gain: 1.4464393446710155
Gain: 1.4464393446710155

Information gain: 0.12451124978365291

Same way we need to calculate the entropy and information gain for next record sets then we get

(ii) Column [1]
Calculating gain for record set: [0, 1, 1, 0, 1, 0, 1, 2, 2]
Information gain: 0.5344977967946405

(iii) Column [2]
Calculating gain for record set: [Cheap, Cheap, Cheap, Cheap, Cheap, Standard, Standard, Expensive, Expensive]
Information gain: 1.209865470109874

Column [3]
Calculating gain for record set: [Low, Medium, Medium, Low, Medium, Medium, Medium, High, Medium, High]
Information gain: 0.6954618442383218

4.1.2 Information Gain Table

Next we need to create the information table of FID3
[0.12451124978365291, 0.5344977967946405, 1.209865470109874, 0.6954618442383218]
From this table we get the following information

Highest gain column: 1.209865470109874: column no. 2
Now we can use it to expand the tree.

4.1.3 Define thresholds

If the learning of FDT stops until all the sample data in each leaf node belongs to one class, it is poor in accuracy. In order to improve the accuracy, the learning must be stopped early or termed pruning in general. As a result, two thresholds are defined [8].

(i) Fuzziness control threshold \( \theta_r \)

If the proportion of a data set of a class \( C_i \) is greater than or equal to a threshold \( \theta_r \), stop expanding the tree.
For example: if in sub-dataset the ratio of class 1 is 90%, class 2 is 10% and \( \theta_r \) is 85%, then stop expanding.

(ii) Leaf decision threshold \( \theta_n \)

If the number of a data set is less than a threshold \( \theta_n \), stop expanding.
For example, a data set has 600 examples where \( \theta_n \) is 2%. If the number of samples in a node is less than 12 (2% of 600), then stop expanding.
The level of these thresholds has great influences on the result of the tree. We define them in different levels in our experiment to find optimal values.
Moreover, if there are no more attributes for classification, the algorithm does not create a new node.

4.1.4 The procedure to build the fuzzy decision tree:

Create a Root node that has a fuzzy set of all data with membership value 1. With the result of the calculation above, we use the attribute column no.2 to expand the tree.

Generate two sub-nodes with the examples, where the membership values at these sub-nodes are the product of the original membership values at Root and the membership values of the attribute column no.2. The example is omitted if its membership value is null.

In this way we have implemented the basic decision tree and fuzzy ID3 algorithm in java.
And the results of implementation is presented in terms of information gain, Entropy and decision tree.

5. Comparing the algorithms among ID3, FID3 and PFID3

Because FID3 and PFID3 are based on ID3, these three methodologies have similar algorithms. However, there also exist some differences.

(i) Data representation: The data representation of ID3 is crisp while for FID3 and PFID3, they are fuzzy, with continuous attributes. Moreover, the membership functions of PFID3 must satisfy the condition of well-defined sample space. The sum of all the membership values for all data value \( i x \) must be equal to 1.

(ii) Termination criteria: ID3: if all the samples in a node belong to one class or in other words, if the entropy equals to null, the tree is terminated. Sometimes, people stop learning when the proportion of a class at the node is greater than or equal to a predefined threshold. This is called pruning. The pruned ID3 tree tops early because the redundant branches have been pruned. FID3 & PID3: there are three criteria’s.

1) If the proportion of the dataset of a class is greater than or equal to a threshold \( \theta_r \) stop expanding.
2) If the number of a data set is less than another threshold \( \theta_n \) stop expanding.
3) If there are no more attributes at the node to be classified if one of these three criteria’s is fulfilled, the
learning is terminated.

6. Conclusion

We have given the results of ID3, FID3 from this we conclude that applying the well-defined sample space to the fuzzy partition have a positive effect on the performance. Fuzzy decision tree is an extension of classical decision tree to extract the knowledge in uncertain classification problems. The main difference between the learning ID3 and FID3 is that for discrete values ID3 works well but for continues values it will not give more accuracy. Fuzzy ID3 resolves this problem of uncertainty as per the values shown. Classical decision tree has two issues like How to choose the best criteria to split the training instances and what the stopping rule is to terminate the splitting procedure. These two issues are solved with the help of fuzzy decision tree.

On the contrary, the data point of FID3 can be overweight or underweight. Thus, the learning is inaccurate due to the imbalanced weight of the data. This will be the future scope for further enhancement.

We implemented the system which is based on ID3 and FID3 and result are shown in experiments and results part.

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